# Variational Calculations of Highly Excited Rovibrational States for the Ground Electronic State of $N_2O$

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**ABSTRACT** Variational calculations are presented for highly excited vibrational bound states of  $N_2O$  using a newly constructed *ab initio* multireference configuration interaction potential energy surface. The calculations are performed using a Jacobi coordinate system. The vibrational energies are compared with experimental data and the sources of the discrepancy between them are discussed.

**ABSTRAK** Pengiraan variasi dipersembahkan untuk keadaan-keadaan getaran teruja tinggi bagi  $N_2O$  menggunakan satu permukaan *ab initio* tenaga keupayaan interaksi konfigurasi multirujukan yang baru dibina. Pengiraan dibuat menggunakan satu sistem koordinat Jacobi. Tenaga-tenaga getaran dibandingkan dengan data eksperimen dan sumber-sumber perbezaan antara mereka dibincangkan.

(Variational, multireference configuration interaction, potential energy surface, Jacobi coordinate, rovibrational energy)

### INTRODUCTION

The ground electronic state,  $X^1A'$ , of the N<sub>2</sub>O molecule has been extensively studied throughout the years, both theoretically and experimentally. The experimental study of the IR of N<sub>2</sub>O molecule has been intensified in the last 20 years. Amiot and Guelachvili [1, 2] have recorded infrared spectrum of this molecule which cover the spectral region up to 8200 cm<sup>-1</sup> using Fourier Transform spectroscopy. Campargue et al. [3] have completed the analysis of the FT spectrum of N<sub>2</sub>O in the near infrared and visible region and have extended it up to 11 000 cm<sup>-1</sup>. This group has also reported the spectrum for a number of bands of N<sub>2</sub>O using intracavity laser spectroscopy between 11 700 and 15 000 cm<sup>-1</sup>. Various potential energy surfaces have been determined for this state, including empirical fits as those performed by Lacy et al. [4], Kobayashi et al. [5] and Teffo et al. [6], and also the *ab initio* calculation carried out by Martin et al. [7] and Csaszar et al. [8]. Some of these surfaces have been used to investigate the vibrational spectrum of N<sub>2</sub>O. Zuniga et al. [9] have considered these issues by

performing extensive variational calculations of highly excited state up to 15 000 cm<sup>-1</sup>. A great variety of curvilinear vibrational coordinates have been used to calculate vibrational energies of N<sub>2</sub>O such as Radau and hyperspherical coordinates. With a systematic way of adjusting fitted potential energy functions together with the most sophisticated variational methods employed to calculate vibrational energies, all the reported results give excellent agreement when compared to observed values.

This paper presents the two dimensional variational calculations of highly excited vibrational states of  $N_2O$  molecule using the recently derived *ab initio* potential energy surface. The surface is interpolated using the spline method and the quality of the interpolated potential energy surface is checked by comparing the calculated vibrational energies with the experimental frequencies.

#### THEORY

The quantum mechanical characterisation of a molecular system can be formulated either time-

independently or time-dependently. The timeindependent approach is based on the timeindependent Schrödinger equation:

H

$$\Psi = E\Psi$$

where in the current case,  $\hat{H}$  is the rovibrational Hamiltonian of the system. The eigenvalues and eigenfunctions of  $\hat{H}$  can be obtained using the Rayleigh variational principle which leads to the direct diagonalisation of the Hamiltonian matrix. The resultant eigenvalues provide information on the rovibrational spectrum of the system.

The relevant coordinates employed for the body-fixed (rotating) frame are the Jacobi coordinates  $(R, r, \theta)$  as depicted in Figure 1. The three Euler angles ( $\omega \equiv \alpha, \beta, \gamma$ ) define the orientation of the body-fixed axes (x, y, z) with respect to the space-fixed (non-rotating) axes (X, Y, Z). The nuclear Hamiltonian operator for a triatomic molecule in the Jacobi coordinates system is expressed as [10, 11]

$$\hat{H} = \left\{ -\frac{\hbar^2}{2\mu} \frac{\partial^2}{\partial R^2} - \frac{\hbar^2}{2\mu_r} \frac{\partial^2}{\partial r^2} \right\} - \left( \frac{\hbar^2}{2\mu R^2} - \frac{\hbar^2}{2\mu_r r^2} \right) \times \left\{ \frac{1}{\sin\theta} \frac{\partial}{\partial\theta} \sin\theta \frac{\partial}{\partial\theta} - \frac{K^2}{\sin^2\theta} \right\} + V(R, r, \theta) \Phi^{JK}(R, r, \theta, t)$$
(1)  
$$+ \left( \frac{\hbar^2}{2\mu R^2} \right) \left( J \left( J + 1 \right) - 2K^2 \right) - \frac{\hbar^2 C_{JK}^{-1}}{2\mu R^2} \left\{ \frac{\partial}{\partial\theta} - K \cot\theta \right\} - \frac{\hbar^2 C_{JK}^{-1}}{2\mu R^2} \left\{ -\frac{\partial}{\partial\theta} - K \cot\theta \right\}$$

where

 $C_{JK}^{\pm} = \left[J \left(J + 1\right) - K \left(K \pm 1\right)\right]^{1/2},$ 

V is the electronic potential energy, J is the total angular momentum quantum number, and K is the quantum number for the projections of J and of j onto the body-fixed z axis. K is the so-called the helicity angular momentum quantum number.

The nuclear wavefunction corresponding to a particular J and M can be expressed in the form of [10, 12, 13]

$$\Psi^{J,M,p}(R,r,\theta,\omega) = \sum_{K=\lambda}^{J} \Phi^{J,K,p}(R,r,\theta) \times |J,K,M,p\rangle$$
(2)

where M is the quantum number for the projection of **J** onto the space-fixed Z axis and  $\lambda$  is defined as

$$\lambda = \frac{1 - (-1)^{J+p}}{2}.$$
 (3)

The parity adapted body-fixed angular momentum basis functions in eq. (2) is defined as

$$|J, K, M, p\rangle = \sqrt{\frac{2J+1}{8\pi^2} \frac{1}{\sqrt{2(1+\delta_{0,K})}}}$$

$$\times \left[ D_{K,M}^J(\omega) + (-1)^{J+K+p} D_{-K,M}^J(\omega) \right]$$
(4)
where  $D_{-K,M}^J(\omega)$  indicates the retation matrices of

where  $D_{K,M}^{J}$  indicates the rotation matrix of Wigner *D*-functions.

 $\lambda = K_{\min}$  in eq. (3) takes on the value of 0 or 1, depending on the value of  $(-1)^{J+p}$  where p = 1and p = 2 correspond to the states of odd parity and even parity, respectively. For  $K \neq 0$ , p takes on the value of 1 or 2. For K = 0, p takes on only the value of 2 because if J = 0, the only possible value of  $\lambda$  is 0. For a given J, there exist 2J + 1 wavefunctions which correspond to different K. The K and -K terms have been grouped together in one parity-adapted wavefunction (see eq. (4)). Therefore, the 2J +1 fold degenerate of K states can now be divided into a set of J + 1 fold degenerate with  $K = 0, 1, 2, 3, \dots, J$  for even parity states (p =2) and a set of J fold degenerate states with K $= 1, 2, 3, \dots, J$  for odd parity states (p = 1).

Notations of  $v_1$ ,  $v_2$  and  $v_3$  are used to denote vibrational quanta for the N<sub>2</sub>-O stretching, N<sub>2</sub>-O bending and N-NO stretching, respectively. The notation of  $(v_1, v_2^{|l|}, v_3)$  is used for the degenerate states of  $(v_1, v_2, v_3)$ , distinguished by a vibrational angular momentum l that the allowed values of l are connected with the bending quantum numbers,  $v_2$ , by  $l = -v_2$ ,  $-v_2 + v_3$ 2, ...,  $+v_2$ . The allowed values of the total angular momentum quantum number J are connected with l by  $J = |l|, |l| + 1, \dots$ Accordingly, to compute the rotationalvibrational energy and wavefunction for a state with an odd bending quantum number, we considered J = 1 with parity state either odd or even. For an odd parity state, the allowed Kvalues are 0 and 1, while for an even parity state the allowed K value is 0. For a state with an even bending quantum number, we considered J = 0 with even parity state where J = 0 with

odd parity state is symmetry forbidden. Since the total angular momentum, J, and parity are good quantum numbers, the bound state computations were performed separately for different values of J and parity. On the other hand, the helicity quantum number K is not conserved and different values of K were coupled.

A uniform grid was used for the coordinate Rand the action of the associated kinetic energy operator on the bound state wavefunction is evaluated using fast Fourier transforms [14, 15]. The radial kinetic energy operator is diagonal in momentum space. For this reason, the wavefunction is transformed to its momentum representation via the fast Fourier transform technique

$$\Phi^{J,K,p}(k_R,r,\theta) = \frac{1}{\sqrt{2\pi}} \int_0^\infty \exp\left(-ik_R R\right) \\ \times \Phi^{J,K,p}(R,r,\theta) dR$$
$$\Phi^{J,K,p}(R,r,\theta) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^\infty \exp\left(ik_R R\right) \\ \times \Phi^{J,K,p}(k_R,r,\theta) dk_R,$$

multiplied by the kinetic energy at the each momentum grid point

$$\begin{cases} -\frac{\hbar^2}{2\mu} \frac{\partial^2}{\partial R^2} \\ \end{bmatrix} \Phi^{J,K,p} (R,r,\theta) \\ = \begin{cases} -\frac{\hbar^2}{2\mu} \frac{\partial^2}{\partial R^2} \\ \end{pmatrix} \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \exp\left(ik_R R\right) \\ \times \Phi^{J,K,p} (k_R,r,\theta) dk_R \\ = \begin{cases} \frac{\hbar^2}{2\mu} \\ \end{cases} \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} k_R^2 \exp\left(ik_R R\right) \\ \end{bmatrix}$$

 $\times \Phi^{J,K,p}\left(k_{R},r,\theta\right)dk_{R}$ 

and transformed back to the coordinate representation

$$\begin{cases} -\frac{\hbar^2}{2\mu} \frac{\partial^2}{\partial R^2} \} \Phi^{J,K,p} (R,r,\theta) \\ = \left\{ \frac{\hbar^2}{2\mu} \right\} \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} k_R^2 \exp \left( ik_R R \right) \\ \times \Phi^{J,K,p} \left( k_R, r, \theta \right) dk_R \\ = \left\{ \frac{\hbar^2}{2\mu} \right\} \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} k_R^2 \exp \left( ik_R R \right) \\ \times \frac{1}{\sqrt{2\pi}} \int_{0}^{\infty} \exp \left( -ik_R R' \right) \\ \times \Phi^{J,K,p} \left( R', r, \theta \right) dR' dk_R. \end{cases}$$

A grid or discrete variable representation (DVR) approach [16] was used to evaluate the action of



Figure 1. Jacobi coordinates used in the potential energy and dynamics calculations: r denotes the bond distance of the N<sub>2</sub> diatomic; R denotes the bond distance between the centre of mass of N<sub>2</sub> diatomic and O atom;  $\theta$  denotes the N<sub>2</sub>-O Jacobi angle.

The angular part of the kinetic energy operator on the bound state wavefunction, and consequently the angular grid points correspond to Gauss-Legendre quadrature points. In order to perform this operation, we expand the wavefunction in terms of normalised associated Legendre polynomials

$$\Phi^{J,K,p}(R,r,\theta) = \sum_{j} \Phi^{J,K}_{j}(R,r) \Theta_{jK}(\theta)$$

and use the fact that the associated Legendre polynomials are eigenfunctions of the operator for the first angular term

$$-\left(\frac{\hbar^2}{2\mu R^2} - \frac{\hbar^2}{2\mu_r r^2}\right) \times \left\{\frac{1}{\sin\theta}\frac{\partial}{\partial\theta}\sin\theta\frac{\partial}{\partial\theta} - \frac{K^2}{\sin^2\theta}\right\}\Theta_{jK}(\theta) \\ = \hbar^2 j(j+1)\Theta_{jK}(\theta)$$

Corey and Lemoine [17] have discussed how a single set of angular grid points are used in conjunction with the associated Legendre polynomials, corresponding to different K values. The grid representation for the wavefunction is therefore

 $\bar{\Phi}^{J,K}(R_i, r_j, \theta_\alpha) = \sqrt{w_\alpha} \Phi^{J,K}(R_i, r_j, \theta_\alpha)$ where  $w_\alpha = \sin \theta_\alpha$  are the Gauss-Legendre weights and  $\theta_\alpha$  are the grid points. The normalised associated Legendre functions constitute our fixed basis representation (FBR). The transformation matrix from the DVR to the FBR representation is given by

$$T_{j\alpha}^{K} = \sqrt{w_{\alpha}}\Theta_{jK}\left(\theta_{\alpha}\right)$$

Using these equations, we can write one term in the expansion of the wavefunction in terms of the associated Legendre polynomials as Malaysian Journal of Science 27 (2): 123 – 130 (2008)

$$\Phi_{j}^{J,K}(R_{i},r_{j})\Theta_{jK}(\theta) = \sum_{\alpha}T_{j\alpha}^{K} \times \bar{\Phi}^{J,K}(R_{i},r_{j},\theta_{\alpha})$$

Since the potential energy is diagonal in coordinate space, its action on the wavefunction involves just the multiplication of the values of potential with those of wavefunction at the same spatial grid points.

#### **RESULTS AND DISCUSSIONS**



**Figure 2.** Contour plot of the ground electronic state,  $X^1 A'({}^1\Sigma^+)$ , of N<sub>2</sub>O at a fixed ground state equilibrium geometry,  $r_{N-NO} = 2.13199$  Bohr. The energies are plotted in eV relative to the minimum of the ground electronic state. The contours spacing are 0.15 eV.

Ab initio calculations of the singlet potential energy surface of the ground electronic state were performed with the MOLPRO package [18] on the Bristol Beowulf cluster systems consisting of two 2.8 GHz Xeon CPUs with 2.0 GB RAM. The final results presented here are produced using the internally contracted multireference configuration interaction (MRCI) method including the Davidson correction with an AVQZ basis set [19]. The bulk of the calculations are done using  $C_s$  symmetry. The MRCI calculations were preceded by complete active space self consistent field (CASSCF) calculations using an active space that included nine orbitals arising from the 2p atomic orbitals of oxygen and nitrogen, respectively. Figure 2 displays a cut through of the potential energy surface of N<sub>2</sub>O molecule by fixing one of its internal coordinates at ground state equilibrium geometry.



**Figure 3.** Convergence of the  $(0, 2^0, 0)$ ,  $(3, 6^0, 0)$  and  $(6, 0^0, 0)$  rotational-vibrational eigenvalues (energies) with the number of the basis functions.  $N_1$ ,  $N_2$ ,  $N_3$ ,  $N_4$ ,  $N_5$ ,  $N_6$ , and  $N_7$  correspond to the basis functions of  $n_R = 8$  and  $n_{\theta} = 4$ ,  $n_R = 12$  and  $n_{\theta} = 6$ ,  $n_R = 16$  and  $n_{\theta} = 8$ ,  $n_R = 20$  and  $n_{\theta} = 10$ ,  $n_R = 22$  and  $n_{\theta} = 12$ ,  $n_R = 24$  and  $n_{\theta} = 14$ , and  $n_R = 26$  and  $n_{\theta} = 16$ , respectively.



Figure 4. Contour plots of the pure bending vibrational wavefunction for the  $(0, 12^0, 0)$  with J = 0 (even parity) and for the  $(0, 9^1, 0)$  with J = 1 (odd or even parity)

The dynamics calculations were performed on the personal computer consisting of 2.4 GHz Intel Pentium Core 2 Duo CPU with 2.0 GB



1 1

Figure 5. Contour plot of the pure stretching vibrational wavefunction for the  $(6, 0^0, 0)$  with J = 0 (even parity)

RAM. There were 64 angular grid points and 384 radial grid points used in the current work. The radial  $(n_R)$  and angular  $(n_\theta)$  basis functions used consisted of 26 number of terms in Legendre polynomials and 16 number of terms in momentum representation, respectively. With the size of basis functions and grid points, the computed two-dimensional vibrational energies were tested for convergence which has been found to converge up to third decimal places. Figure 3(a) shows that by fixing the grid point at 64 and 384, the  $(0, 2^{\circ}, 0)$  vibrational energy converges from 1160.231281 cm<sup>-1</sup> to 1160.230832 cm<sup>-1</sup> as the basis functions increases from  $n_R = 24$  and  $n_{\theta} = 14$  (N<sub>6</sub>) to  $n_R$ = 26 and  $n_{\theta}$  = 16 (N<sub>7</sub>). Figure 3(b) show that the  $(3, 2^0, 0)$  vibrational energy level converges from 5051.447847 cm<sup>-1</sup> ( $N_6$ ) to 5051.447676  $\operatorname{cm}^{-1}(N_7)$  and (6, 0<sup>0</sup>, 0) vibrational energy level converges from 7611.300399 cm<sup>-1</sup> ( $N_6$ ) to 7611.299804 cm<sup>-1</sup> ( $N_7$ ). Also observable in Figure 3, the lower vibrational energy of  $(0, 2^0, 2^0)$ 0) state converges much faster than the higher vibrational state. By using a small basis set size of  $n_R = 8$  and  $n_{\theta} = 4$ , the (0, 2<sup>0</sup>, 0) vibrational energy shows a sufficiently converged value. The assignments of the states were made by visual inspection of the vibrational





wavefunctions. As examples we show in Figures 4, 5 and 6, the wavefunction contour plots corresponding to the pure bending

vibrational mode, pure stretching vibrational mode and coupled bending-stretching vibrational mode, with one of the internal coordinates kept fixed at its equilibrium value.

**Table 1.** Comparison between calculated and experimental vibrational energies (cm<sup>-1</sup>) for the  $X^{1}A'$  ground state of N<sub>2</sub>O with total angular momentum, J = 0 (even parity)

momentum, $J = 0$ (even parity)				
$v_1, v_2^{ l }, v_3$	$\Delta E$ (Theory) <sup><i>a</i></sup>	$\Delta E(\text{Experimental})^b$		
$ \begin{array}{c} 0, 0^{0}, 0\\ 0, 2^{0}, 0\\ 1, 0^{0}, 0 \end{array} $	0.00	0.00		
$0, 2^{0}, 0$	1160.23	1168.13		
$1, 0^{\circ}, 0$	1269.77	1284.90		
0, 4 <sup>0</sup> , 0	2315.35	2322.57		
$1, 2^{\circ}, 0$	2471.86	2462.00		
∠,∪,∪	2567.08	2563.34		
0.60 0	3450.87	3466.60		
$\begin{array}{c} 1, 4^{0}, 0\\ 2, 2^{0}, 0\\ 3, 0^{0}, 0\end{array}$	3638.51	3620.94		
$2, 2^{0}, 0$	3775.57	3748.25		
$3, 0^{0}, 0$	3857.27	3836.37		
$0, 8^{\circ}, 0$	4589.72			
$1, 6^{\circ}, 0$	4782.02	4767.14		
$2, 4^{\circ}, 0$	4950.45	4910.99		
$3, 2^{0}, 0$	5051.45	5026.30		
$4, 0^{0}, 0$	5130.24	5105.68		
$0, 10^{0}, 0$	5725.79			
$1, 8^{0}, 0$	5936.26			
$2, 6^{\circ}, 0$	6089.22			
$3, 4^{\circ}, 0$	6213.76	6192.27		
$4, 2^{0}, 0$	6291.10	6295.45		
$5, 0^{\circ}, 0$ $0, 12^{\circ}, 0$	6377.79	6373.31		
$0, 12^{0}, 0$	6855.44			
$1, 10^{\circ}, 0$	7068.38			
$2, 8^{\circ}, 0$	7221.43			
$3.6^{\circ}.0$	7335.22			
$4, 4^{0}, 0$	7433.93	7463.96		
$4, 4^{\circ}, 0$ 5, 2°, 0	7504.32	7556.11		
$6, 0^0, 0$	7611.30	7640.45		
$\frac{a}{\Delta E(\text{Theory})} = E(v_1, v_2, v_3) - E(0, 0^0, 0)$				

 $^{a}\Delta E(\text{Theory}) = E(v_1, v_2, v_3) - E(0, 0^{\circ}, 0)$ <sup>b</sup>The experimental values were taken from references [1, 2, 3, 20, 21]

In Table 1 and 2 we compare the calculated values for vibrational energies with those observed experimentally. The tables show the energies corresponding to the states with J = 0 and J = 1, respectively. The first observation is that the agreement between the two sets of results is quite good for some modes while less satisfactory for others, with the maximum discrepancy occurring for the states  $(5, 2^0, 0)$ , with 39.46 cm<sup>-1</sup>, and the minimum discrepancy occurring for the states (2, 0<sup>0</sup>, 0), with 3.74 cm<sup>-1</sup>. For those theoretical values that can be compared with the experimental results, the

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root-mean-square deviations is 21.98 cm<sup>-1</sup> for the 28 vibrational energy levels arising from N<sub>2</sub>O molecules with J = 0 and J = 1.

**Table 2.** Comparison between calculated and experimental vibrational energies (cm<sup>-1</sup>) for the  $X^{1}A'$  ground state of N<sub>2</sub>O with total angular momentum, J = 1 (even or odd parity).

		<u> </u>
$v_1, v_2^{[l]}, v_3$	$\Delta E$ (Theory) <sup><i>a</i></sup>	$\Delta E(\text{Experimental})^{b}$
$0, 1^1, 0$	583.67	588.77
$0, 3^{1}, 0$	1728.10	1749.07
$1, 1^{1}, 0$	1894.98	1880.27
$0, 5^{1}, 0$	2885.45	2897.81
1, 3 <sup>1</sup> , 0	3053.09	3046.21
$2, 1^1, 0$	3191.50	3165.86
$0, 7^{1}, 0$	4022.55	
$1, 5^{1}, 0$	4207.96	4197.96
$2, 3^{1}, 0$	4368.04	4335.80
$3, 1^{1}, 0$	4474.85	4446.38
$0, 9^1, 0$	5051.44	
$1, 7^{1}, 0$	5164.61	
$2, 5^1, 0$	5360.15	
(A E)/(D) = -	1) 77(	

 ${}^{a}\Delta E(\text{Theory}) = E(v_1, v_2, v_3) - E(0, 0^0, 0)$  ${}^{b}\text{The experimental values were taken from references [1, 2, 3, 20, 21].}$ 

The first and second vibrational excited states in the current two-dimensional case can be assigned to excitation of the pure bending motion,  $(0, 1^1, 0)$  and  $(0, 2^0, 0)$ . The differences of these transition energies with the experimental values are 5.1 cm<sup>-1</sup> and 7.9 cm<sup>-1</sup>, respectively, showing that for these motions the coupling between  $\theta$  and r is of little important. This is supported by the fact that the seventh excitation belongs to the stretching normal mode of the  $(1, 0^0, 0)$  state, as previously reported by several workers in the experimental measurements and in the three-dimensional calculations. Therefore, we can expect that the coupling between  $\theta$  and r is negligibly small at least for the two lowest pure bending vibrations of the ground electronic state of N<sub>2</sub>O. For higher pure bending vibrations, they show significant discrepancies with the experimental values, for instance, the maximum discrepancy comes from the state  $(0, 3^0, 0)$  which differs by 20.97 cm<sup>-1</sup>. This is a significant difference, resulting from the coupling of r and  $\theta$  in the kinetic energy operator and the coupling need to be considered in the calculation.

The third excitation belongs to the motion along  $R \ (\Delta E = 1269.77 \text{ cm}^{-1})$  which is the stretching

normal mode of  $(1, 0^0, 0)$  state. There is a significant difference with the experimental normal mode frequency, with the calculated value underestimated by 15.13 cm<sup>-1</sup>. As observed, the greatest difference comes from the state  $(4, 0^0, 0)$ , with 21.49 cm<sup>-1</sup>. The first coupled stretching and bending excitation corresponds to the  $(1, 1^1, 0)$  state and its vibrational energy differs by 14.71 cm<sup>-1</sup> from that of the observed value. The maximum discrepancy comes from the states  $(5, 2^0, 0)$  which is also the source of the greatest error in the theoretical calculations.

#### CONCLUSION

In general, the agreement between the computed and the experimental values is good for low vibrational energies. Nevertheless, at any rate it becomes apparent from these results that a three-dimensional treatment of the vibrational energy level calculations for N<sub>2</sub>O is needed for higher vibrational excitations in which anharmonicity and the coupling between the different motions cannot be neglected. Such a computation would require an order of magnitude more computational facilities than were used here. This aspect will be considered in our future work. Due to the fact that the vibration of the N-NO bond is expected to play only a minor role in the photolysis process, it is enough to consider only two-dimensional treatment in the calculations. This assumption is supported from previous experimental finding that at room temperature, the first ultraviolet absorption band arises from excitations starting from the three lowest vibrational energy levels of ground electronic state and the population of these levels accounts for more than 99% of the N<sub>2</sub>O ground state vibrational population.

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#### REFERENCES

 Amiot, C. and Guelachvili, G. (1974). Vibration-rotation bands of <sup>14</sup>N<sub>2</sub><sup>16</sup>O: 1.2 micron - 3.3 micron region. J. Mol. Spectrosc. 51: 475.

- 2. Amiot, C. and Guelachvili, G. (1976). Extension of the  $10^6$  samples Fourier spectrometry to the Indium Antimonide region: Vibration-rotation bands of  ${}^{14}N_2{}^{16}O$ : 3.3-5.5  $\mu$ m region. J. Mol. Spectrosc. 59: 171.
- Campargue, A., Permogorov, D., Bach, M., Temsamani, M., Auwera, J. V. and Fujii, M. (1995). Overtone spectroscopy in nitrous oxide. J. Chem. Phys. 103: 5931.
- Lacy, M. and Whiffen, D. H. (1982). The anharmonic force field of nitrous oxide. *Mol. Phys.* 45: 241.
- Kobayashi, M. and Suzuki, I. (1987). Sextic force field of nitrous oxide. J. Mol. Spectrosc. 125: 24.
- Teffo, J. L. and Chedin, A. (1989). Internuclear potential and equilibrium structure of the nitrous oxide molecule from rovibrational data. J. Mol. Spectrosc. 135: 389.
- Martin, J. M. L., Taylor, P. R. and Lee, T. J. (1993). Accurate ab initio quartic force fields for the N<sub>2</sub>O and CO<sub>2</sub> molecules. *Chem. Phys. Lett.* 205: 535.
- Csaszar, A. G. (1994). Anharmonic Force Field of N<sub>2</sub>O. J. Phys. Chem. 98: 8823.
- Zúñiga, J., Alacid, M., Bastida, A., Carvajal, F. J. and Requena, A. (1999). Determination of highly excited rovibrational states for N<sub>2</sub>O using generalized internal coordinates. J. Chem. Phys. 110: 6339.
- 10. Balint-Kurti, G. G. (2003). Wavepacket theory of photodissociation and reactive scattering. *Adv. Chem. Phys.* **128**: 249.
- 11. Offer, C. C. and Balint-Kurti, G. G. (1994). Time-dependent quantum mechanical study of the photodissociation of HOCl and DOCl. J. Chem. Phys. **101**: 10416.
- 12. Balint-Kurti, G. G. and Brown, A. (2004). Time-dependent wavepacket calculations for reactive scattering and photodissociation. *Theory of Chemical Reaction Dynamics*, Kluwer Academic Publishers: 149.
- Balint-Kurti, G. G., Füsti-Molnár, L. and Brown, A. (2001). Photodissociation of DOBr - Time-dependent wavepacket

calculations. Phys. Chem. Chem. Phys. 3: 702.

- Kosloff, R. (1988). Time-dependent quantum-mechanical methods for molecular dynamics. J. Phys. Chem. 92: 2087.
- Balint-Kurti, G. G., Dixon, R. N. and Marston, C. C. (1992). Grid methods for solving the schrödinger equation and time dependent quantum dynamics of molecular photofragmentation and reactive scattering processes. *Int. Rev. Phys. Chem.* 11: 317.
- Light, J. C., Hamilton, I. P. and Lill, V. J. (1985). Generalized discrete variable approximation in quantum mechanics. J. Chem. Phys. 82: 1400.
- 17. Corey, G. and Lemoine, D. (1992). Pseudospectral method for solving the time-dependent Schrödinger equation in spherical coordinates. J. Chem. Phys. 97: 4115.
- MOLPRO, a package of *ab initio* programs designed by Werner, H. -J. and Knowles, P. J. version 2002.1, Amos, R. D., Bernhardsson, A., Berning, A., Celani, P., Cooper, D. L., Deegan, M. J. O., Dobbyn, A. J., Eckert, F., Hampel, C., Hetzer, G., Knowles, P. J., Korona, T., Lindh, R., Lloyd, A. W., McNicholas, S. J., Manby, F. R., Meyer, W., Mura, M. E., Nicklass, A., Palmieri, P., Pitzer, R., Rauhut, G., Schütz, M., Schumann, U., Stoll, H., Stone, A. J., Tarroni, R., Thorsteinsson, T. and Werner, H. -J.
- Dunning, Jr., T. H. (1989). Gaussian basis sets for use in correlated molecular calculations. I. The atoms boron through neon and hydrogen. J. Chem. Phys. 90: 1007.
- Toth, R. A. (1991). Line-frequency measurements and analysis of N<sub>2</sub>O between 900 and 4700 cm<sup>-1</sup>. Appl. Opt. **30**: 5289.
- 21. Campargue, A. (1996). The near-infrared absorption spectrum of nitrous oxide: analysis of the  $5v_3$  and  $v_1 + 5v_3$  clusters. *Chem. Phys. Lett.* **259**: 563.